

$$E(a + bY) = a + bE(Y)$$

$$\text{var}(a + bY) = b^2 \text{var}(Y)$$

$$a + bY = -\lambda^2 Y$$

$$a = 0$$

$$b = -\lambda^2$$

$$b^2 \text{var}(Y) = (-\lambda^2)^2 \left(\frac{1}{\lambda^2}\right) = \lambda^2$$

$X_1, X_2, \dots, X_n \stackrel{i.i.d.}{\sim} \text{Poi}(\mu)$

$$\bar{X}_n \approx \text{Normal}(\mu, \mu)$$

$$g(x) = \sin(x)$$

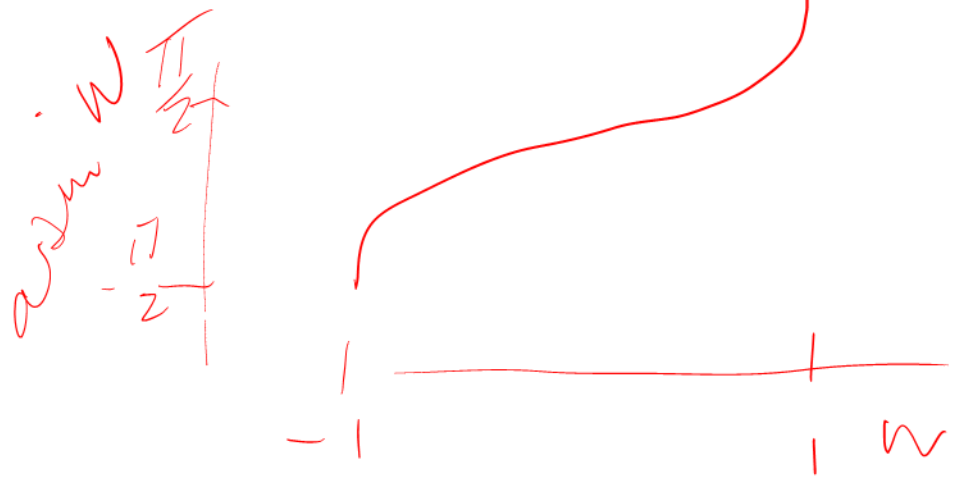
$$g'(x) = \cos(x)$$

$$g(\bar{X}_n) = \sin(\bar{X}_n)$$

$$\approx \mathcal{N}\left(g(\mu), \frac{[g'(\mu)]^2 \sigma^2}{n}\right)$$

$$= \mathcal{N}\left(\sin(\mu), \frac{\cos^2(\mu) \cdot \mu}{n}\right)$$

μ may be
function of
other parameters



$$E(X) = \frac{1-p}{p}$$

$$\text{Var}(X) = \frac{1-p}{p^2}$$

$$\frac{1-p}{p} = \mu$$

$$1-p = p\mu$$

$$1 = p\mu + p$$

$$= p(1+\mu)$$

$$\text{Var}(\mu) = \frac{1-p}{p^2} = \frac{1 - \left(\frac{1}{1+\mu}\right)}{\left(\frac{1}{1+\mu}\right)^2}$$

$$p = \frac{1}{1+\mu}$$

$$\begin{aligned} &= (1+\mu)^2 \left[1 - \frac{1}{1+\mu} \right] = (1+\mu)^2 - (1+\mu) \\ &= (1+\mu)(1+\mu-1) \\ &= \mu(1+\mu) \end{aligned}$$